

```
DSolve[
{
  D[g[t, a], t] == h (a - b) D[g[t, a], a],
  g[0, a] == a
},
g[t, a],
{t, a}
]
{{g[t, a] -> b + a e^{ht} - b e^{ht}}}
```